

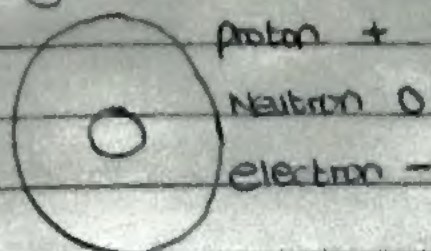
19/06/14

ELECTROSTATIC

There are two kind of Charges

+ positive charges

- Negative charges.



Electron Charges magnitude.

$$3e = - - -$$

$$1e = 1.602 \times 10^{-19} \text{ C}$$

$$3p = + + +$$

$$1p = +1.602 \times 10^{-19} \text{ C.}$$

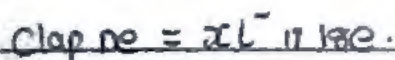
A -ve charge & -ve charge will repel each other

A +ve charge & +ve charge will repel each other

A +ve & -ve will attract each other.

- The atom in its natural state is neutral.

The process of moving or removing an electron in an atom is called Ionization.



Unit = Coulomb = C

$$1C = 6$$

$$q = 1.60 \times 10^{-19}$$

$$\text{Object } q = \frac{8.0 \times 10^{-19} \text{ C}}{1.6 \times 10^{-19}} \approx 5e.$$

The electrostatic force is an attractive force it binds. The proton & the electron

together & make them to co exist.

The Coulombs law state the electric force b/w two charge particle which are stationary is proportional to d product of d charge.

∴ Coulombs Law

$$F \propto \frac{q_1 q_2}{r^2}$$

Ex:- Asst Like charges repels while Unlike charges attract.

proportional to d product of d charge the force can be positive or negative.

eg:- The electron & proton in an hydrogen atom are represented by

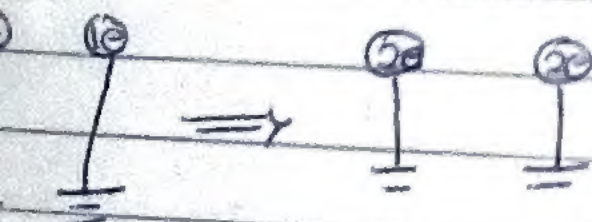
$$r = 5.3 \times 10^{-19} \text{ m}$$

and d magnitude of d force.

$$q^+ \rightarrow q^-$$

$$F = \frac{k_e |q^+| |q^-|}{r^2} = \frac{9 \times 10^9 (1.60 \times 10^{-19})^2}{(5.3 \times 10^{-11})^2}$$

$$= 8.2 \times 10^{-8} \text{ N}$$



$$3^+ + 1^- = \underline{3^+}$$



$$4^+ + 1^- = \underline{3^+}$$

ELECTROSTATICS

There are two kinds of electric charges, which were given the names positive & negative.

The charge on an atom is determined by a sub-atomic particles that make up



Proton: has a positive charge & is located in the nucleus.

Neutron: has no charge & is neutral & is also located in the nucleus or it is in the spaces b/w the protons.

Electron: has a negative charge & it is located outside of the nucleus in an electric cloud around the atom.

PARTICLE CHARGES

Electron & proton have the same magnitude of charge (elementary charge e).

* Electron $(-e)$: $-1.6 \times 10^{-19} \text{ C}$

* Proton $(+e)$: $+1.6 \times 10^{-19} \text{ C}$.

* This is why electrons are forced to orbit around the nucleus.

* Electrostatic forces hold atoms together.

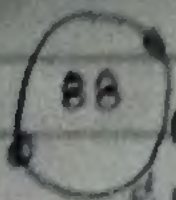
* The Law of charges which states that like charges repel & unlike charges attract.

* A negatively charged rubber rod suspended by a thread is attracted to a positively charged glass rod.

* A negatively charged rubber rod is repelled by another negatively charged rubber rod.

How do atoms become "charged"?

How can this happen?



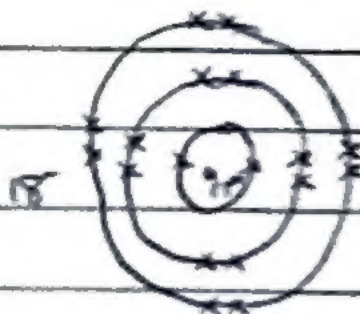
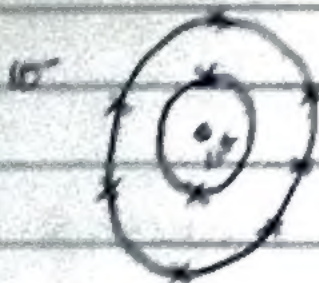
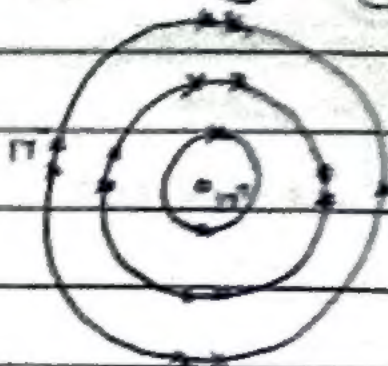
Remove or add a proton or an electron.

Protons & neutrons are bound together by strong nuclear force. It is very hard to separate them. Electrons however, can be more easily removed.

NOTE:

1013?

An atom with a deficiency of electrons is positively charged.



An atom with an excess of electrons is negatively charged.

NOTE: 1. ATOMS DO NOT GAIN OR LOSE PROTONS.

CHARGE IS A FUNDAMENTAL QUALITY LIKE MASS.

Charge is denoted as q .

Charge has a fundamental unit of a Coulomb (C).

Charge are usually really, really small numbers $< 10^{-19}$.

So what is 1C?

An object would have to have 6.25×10^{13} extra electrons in amount +1C of charge.

* A lightning bolt is estimated to carry a charge of 10^6 C.

* Recall the charges on an electron & proton.

CHARGES ARE QUANTIZED, CAN ONLY BE IN MULTIPLES OF e .

Remember:- $-e = \text{an electron} = -1.60 \times 10^{-19} \text{ C}$.

$+e = \text{a proton} = +1.60 \times 10^{-19} \text{ C}$.

* An object that has a net charge of $8.0 \times 10^{-19} \text{ C}$ has a net charge of what multiple of e ? Hint: How many electrons would need to be removed to create this charge?

The net charge would be $+5e$, 5 electrons were removed.

* Two kinds of charges occur in nature, with a property that unlike charges attract one another & like charges repel one another.

* Charge is conserved.

* Charge is quantized.

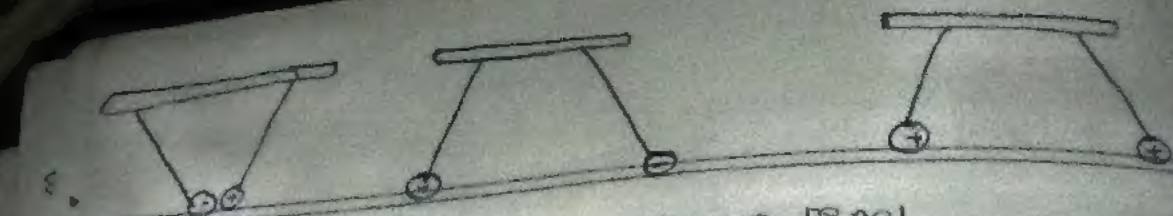
MULTIPLES OF CHARGES CHARGES.

$1e$	1.6×10^{-19}
$2e$	3.2×10^{-19}
$3e$	4.8×10^{-19}
$4e$	6.4×10^{-19}
$5e$	8.0×10^{-19}

ELECTROSTATIC FORCE.

This is a non-contact force & like a gravitational force except instead of two masses exerting force on each other the two objects charges exert a force of repulsion or attraction.

* Any charged object can exert the electrostatic force upon other objects - both charged & uncharged objects.



Object with like charges repel
Object with unlike charges attract

Coulomb's Law

Coulomb confirmed that electric force ~~also~~ ^{between} two small charged spheres is proportional to the ~~inverse~~ ^{inverse square} of their separation distance.

Coulomb's Experiments showed that the electric force between two stationary charged particles:

- Is inversely proportional to the square of the separation between particles and directly along the line joining them.
- Is proportional to the product of the charges q_1 and q_2 on the two particles.

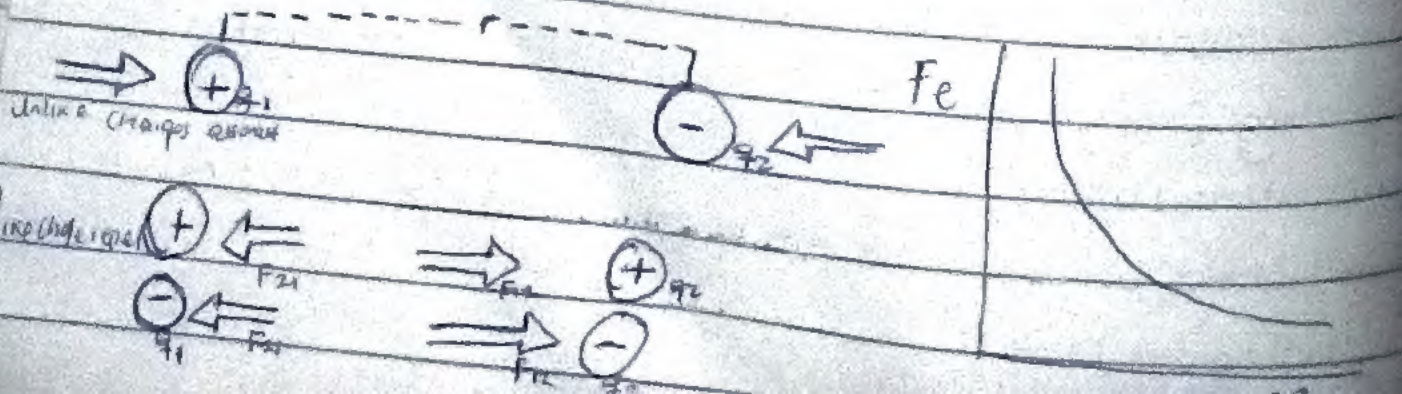
• Is attractive if the charges are of opposite sign and repulsive if the charges have the same sign.

From these observations, we can express Coulomb's Law equation the magnitude of the electric force (sometimes called the Coulomb force) between two point charges:

$$F_e = k_e \frac{|q_1| |q_2|}{r^2} \quad k_e = 1/9 \times 10^9$$

Where k_e is a constant (called Coulomb's constant) $k_e = 8.9875 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$

THE ELECTROSTATIC FORCE



magnitude

$$F_e = \frac{k_e |e|^2}{r^2} = \left(8.99 \times 10^9 \frac{\text{N} \cdot \text{m}^2}{\text{C}^2} \right) \left(\frac{1.60 \times 10^{-19} \text{C}}{5.3 \times 10^{-11} \text{m}} \right)^2$$

$$= 8.2 \times 10^{-8} \text{N}$$

Example of Electrostatic Forces

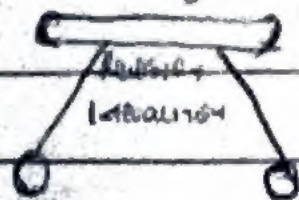
will have a attractive interaction with a neutral object

- A balloon when rubbed on your head become charged by picking up extra electrons from your hair.

- The same balloon, because it is charged, will attract a neutral object like pieces of paper.

So we are able to predict the charge on object based on their interaction

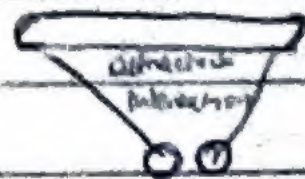
with other object.



Repulsive interaction provides convincing evidence that both objects must be charged.

They can either both be positive or both be negative.

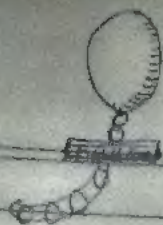
Why does the balloon stick to the wall?



Attractive interaction can lead one to conclude that at least one of the objects is charged.

They can have opposite charges or one object is charged and the other is neutral.

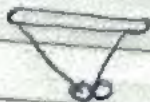
When a balloon is rubbed with a piece of cloth, electrons are transferred to



NOTE: The microscopic makes a wall that is scale with the physical

WHAT HAPPEN TO YOUR HAIR WHEN YOU RUB A BALLOON ON YOUR HEAD?

- The balloon, after being rubbed and then pulled away, removes some of the electrons in your hair which gives each strand a positive charge. Hair charges want to repel and each strand is repelling from the others and "standing up".



GETTING SHOCKED

- As you walk across a carpet, electrons are transferred from the rug to you.
- Now you have extra electrons.
- Tough a door knob (conductor) and ZAP!
- The electrons move from you to the knob.

LIGHTNING

- Lightning is a really big shock.
- Positive charges tend to go up, negatively charges tend to go down.
- When the attraction reaches a critical level you get a lightning bolt.

OBJECT that tend to give up electrons and become ^{positive} ~~negative~~

- * Glass
- * Fur
- * Wool
- * Nylon
- * Hair

OBJECT that tend to attract electron and become negative.

- * Rubber
- * Styrofoam
- * PVC
- * Polyester
- * Saran wrap

INSULATORS AND CONDUCTORS

Different materials hold electrons differently.

- INSULATORS don't let electrons move around within material freely.

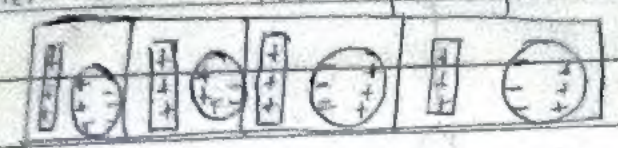
eg. ~~Chalk~~, ~~Plastics~~, ~~Glass~~, ~~Dry air~~, ~~Wood~~, ~~Rubber~~
Conductors - do let electron move around within the material freely. eg.
 Metals, Silver, Copper, Aluminium.

TR1 THIS

• A charged plastic rod is brought close to a neutral metal sphere. How would the distribution of charges be in the metal sphere?



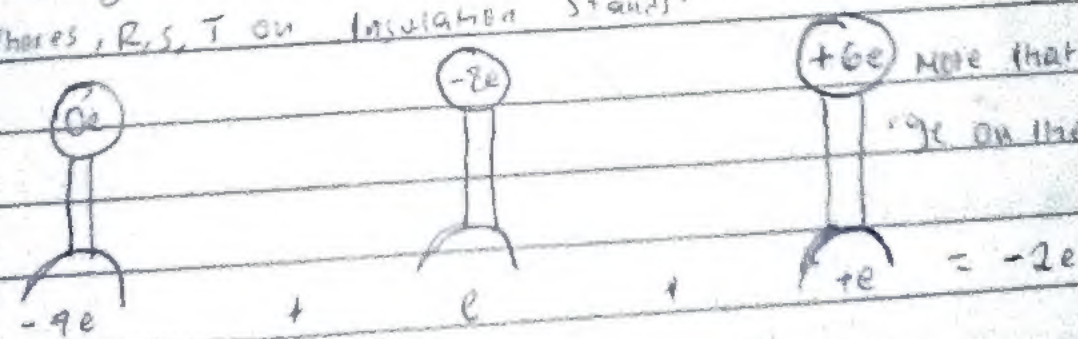
• Which of the diagrams below best represents the charged distribution on a metal sphere when a positively charged plastic tube is placed nearby?



LAW OF CONSERVATION OF CHARGE

• Charge within a closed system may be transferred from one object to another, but charge is neither created nor destroyed.

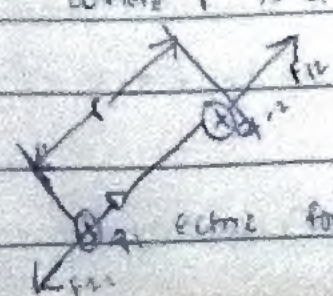
The diagram below shows the initial charges and positions of three metal spheres, R, S, T on insulation stands.



Note that the net charge on the system is $-2e$.

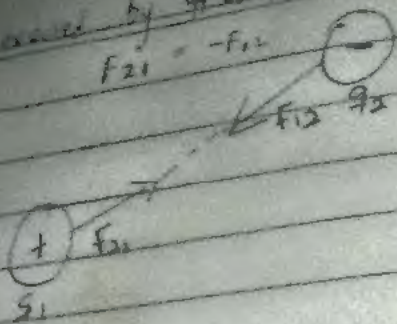
ELECTROSTATIC FORCE IS A VECTOR QUANTITY.

Thus the Coulomb's Law expressed in vector form for the electric force exerted by a charge q_1 on a second charged q_2 , written as is where \hat{r} is a unit vector directed from q_1 to q_2 .



Because the electric force obeys Newton's Third Law the electric force exerted by q_2 on q_1 is equal in magnitude to the

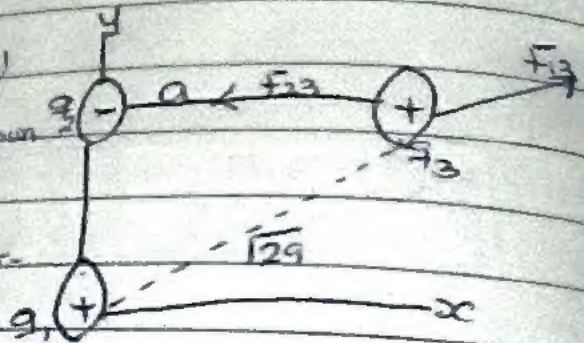
Force exerted by q_1 on q_2 and in the opposite direction; $F_{21} = -F_{12}$



Example 2:

Consider three point charges located at the corners of a right triangle as shown

where $q_1 = q_2 = 5.0 \mu\text{C}$, $q_3 = -2.0 \mu\text{C}$, & $a = 0.10\text{m}$. Find the resultant force exerted on q_3 .



The magnitude of F_{23} is

$$F_{23} = k_e \frac{|q_2||q_3|}{a^2} = \left(\frac{8.99 \times 10^9 \text{ N}\cdot\text{m}^2}{\text{C}^2} \right) \frac{(2.0 \times 10^{-6} \text{ C}) (5.0 \times 10^{-6} \text{ C})}{(0.10 \text{ m})^2}$$

The magnitude of the force exerted by q_1 on q_3 is

$$F_{13} = k_e \frac{|q_1||q_3|}{(\sqrt{2}a)^2} = \left(\frac{8.99 \times 10^9 \text{ N}\cdot\text{m}^2}{\text{C}^2} \right) \frac{(5.0 \times 10^{-6} \text{ C}) (5.0 \times 10^{-6} \text{ C})}{2(0.10 \text{ m})^2} = 11 \text{ N}$$

The force F_{13} is repulsive & makes an angle of 45° with the x axis. Therefore the x & y components of F_{13} are equal, with magnitude given by $F_{13} \cos 45^\circ = 7.79 \text{ N}$.

The force F_{23} is in the negative x direction. Hence the x & y components of

Resultant force acting on q_2 is:

$$F_{ax} = F_{1x} + F_{2x} = 7.94 - 9.05 = -1.11$$

$$F_{ay} = F_{1y} = 7.94$$

We can also express the resulting force acting on q_2 as unit vector form:

$$F_2 = (-1.11\mathbf{i} + 7.94\mathbf{j})\text{N}$$

Example 2:-

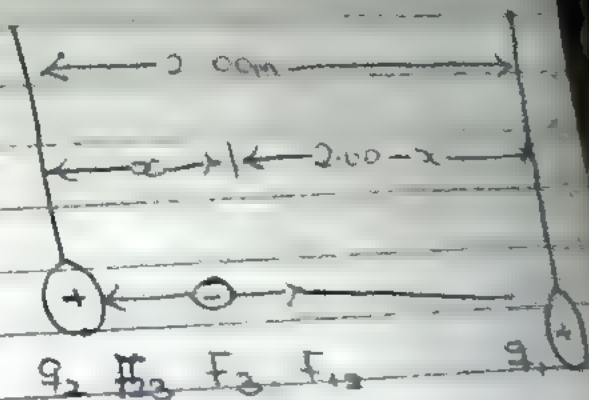
Three point charges lie along the x-axis.

The positive charge $q_1 = 15.0\text{ nC}$ is at $x = 2.00$.

The positive charge $q_2 = 6.00\text{ nC}$ is at the origin.

The negative charge q_3 is at $x = 0$.

What is the x-coordinate of q_3 if the resultant force acting on q_2 is zero?



Solution.

Since q_2 is positive & q_1 & q_3 are positive, the force F_{12} & F_{32} are both attractive, from Coulomb law F_{12} & F_{32} have magnitude:

$$F_{12} = \frac{k_e |q_1| |q_2|}{(2.00-x)^2} = F_{32} = \frac{k_e |q_2| |q_3|}{x^2}$$

For the resulting force on q_2 to be zero

e.g. The electron & proton in a hydrogen atom are represented.

$$r = 5.3 \times 10^{-11}\text{ m}$$

Find the magnitude of the force.

$$q^+ \rightarrow q^-$$

$$F = \frac{k_e |q^+| |q^-|}{r^2} = \frac{8.99 \times 10^{-9} (1.60 \times 10^{-19})^2}{(5.3 \times 10^{-11})^2}$$

$$= 8.2 \times 10^{-8}\text{ N}$$



Electric field & force:

Electric field & force:

Electric dipoles:

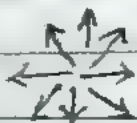
Change particle in E in upper poles:

Electric field region where electric force is expressed as:

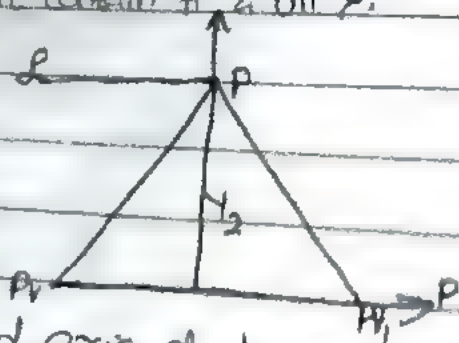
$$F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} = \frac{q_1 q_2}{4\pi\epsilon_0 r^2}$$

$$F = \frac{q}{\epsilon_0}$$

\therefore E of electric field E



Electric dipoles - 2 opposite poles carrying different charges e.g. water molecules
As it contains H^+ & OH^- .



a) Along d axis of dipoles.

b) perpendicular to d axis.

Motion of charge particle in E

$$qE = ma$$

$$a = \frac{qE}{m}$$

Illustration: Charge & electric flux:

→ Gauss law & its application:

* Charge & electric flux

The total of the electric flux out of a ^{close} surface is equal to the charge enclosed divided by the permittivity. The flux per unit area is $\Delta\Phi = \frac{Q}{\epsilon_0 \Delta A}$ $\Delta\Phi$ change in flux; ΔA change in area.

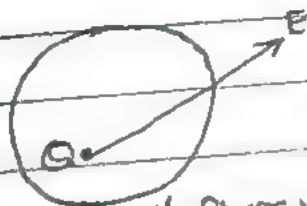
Diagram:-



ϵ_0 Surface area.

$$\text{Flux } \Phi = \frac{Q}{\epsilon_0} \text{ Charge}$$

ϵ_0 permittivity.



The sum of flux is proportional to total charge enclosed.

The electric flux per unit area is defined as electric field multiplied by the area of the surface projected in a plane perpendicular to the field.

"Gauss law is general law applying to any close surface"

* Gauss Law integral;

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q}{\epsilon_0}$$

The area of electric field over any closed surface is equal to the net charge enclosed in the surface divided by the permittivity of space.

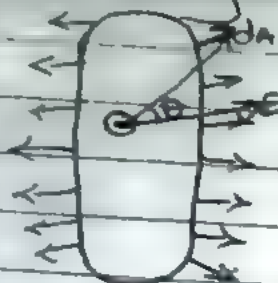
"Gauss law is a form of one of Maxwell's equations, the four fundamental equations for electric & magnetism."

ELECTRIC FLUX.

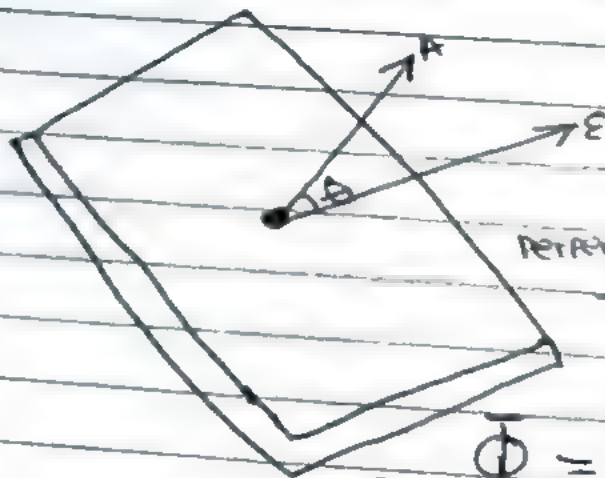
The concept of electric flux is useful in association with Gauss's law. Electric flux through a planar is defined as the electric field multiplied by the component of area perpendicular to the field. If the area is not a plane, then the evaluation of flux generally requires an area integral. Since the angle will be continually changing,

$$\text{Flux} = \Phi = \int E \cos \theta \, dA$$

$$\text{Relative Permittivity} = \epsilon_r = \frac{\epsilon}{\epsilon_0}$$

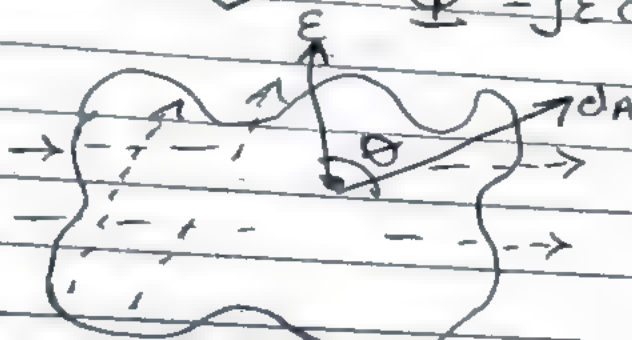


The angle b/w electric field E & area is θ .



Perpendicular
to area.

$$\Phi = \int E \cos \theta \, dA$$



$10^{-12} \rightarrow$ Pico.

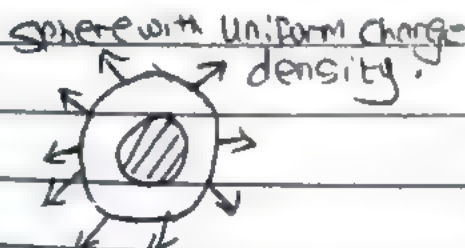
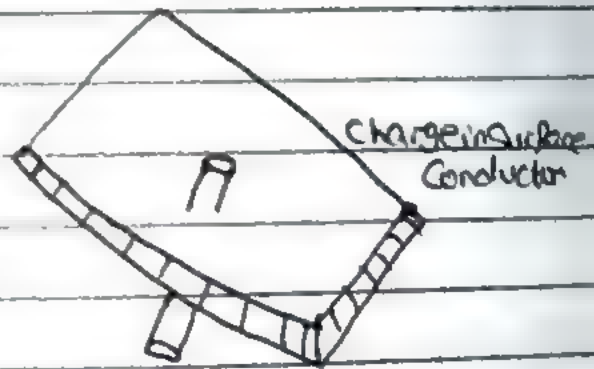
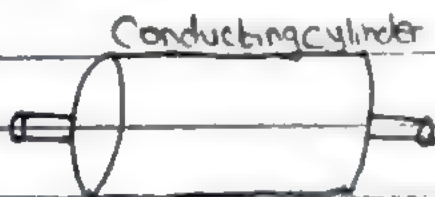
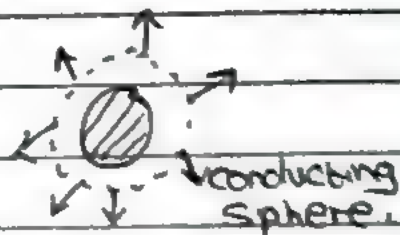
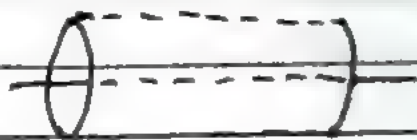
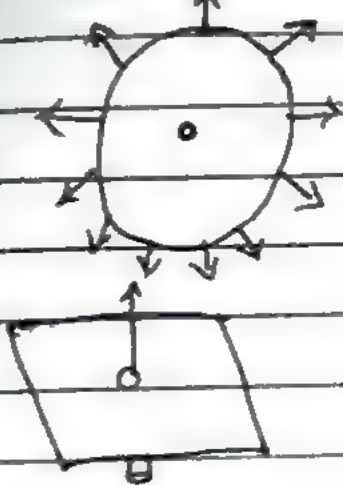
When d area \vec{A} is used in a Vector Operation like this, it is understood that d magnitude of \vec{A} Vector is equal 2 d area & d direction of \vec{A} vector is perpendicular 2 d area.

ϵ_r = permittivity of a medium & dielectric.

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$$

Application of Gauss law.

It is a powerful tool for Calculation of Electric field when they originate from Charge distribution, ^{or} Sufficient symmetry



Cylinder with uniform charge density



charge conducting plates.

Ass

Write four Maxwell's Equation.

Solution:

- Maxwell's Equation are:-
- i) Gauss law.
 - ii) Faraday's law.
 - iii) Electro magnetic induction law.
 - iv) Ampere's law.

Dr. Harmed olamide Sakinudeen

18/03/21

ELECTRIC POTENTIAL:

the potential in

Electric potential means taking a charge from a particular point 2 point within an electric circuit.

$$F = QE$$

$$\therefore E = \frac{F}{Q}$$

$$\Delta V = \frac{\Delta U}{Q}$$

where, Q = charge.

U = Charge in electric potential energy.

V = change in electric potential.

Equipotential Surfaces :- It is a set of point where the electric field is given in the value.

Find E from V

$$E_x = \frac{-\Delta V}{\Delta x}, \quad E_y = \frac{\Delta V}{\Delta y}, \quad E_z = \frac{\Delta V}{\Delta z}$$

potential of a point charge & Groups of point charges

* When is different with electric potential in Electric field

$$V = \frac{W}{q}$$

potential due to a continuous charge distribution
potential energy of system of charges
problems

1. The electric potential difference b/w the ground & a cloud in a particular thunderstorm is $1.2 \times 10^9 \text{ V}$. What is the magnitude of change in energy in multiples of the electron volt?

Soln

$$\Delta U = \frac{\Delta U}{q}$$

$$\Delta U = q \times \Delta V$$

$$= 1.6 \times 10^{19} \times 1.2 \times 10^9 \text{ V}$$

$$= 1.2 \times 10^9 \text{ eV}$$

2. An infinite non conducting sheet has a surface charge density $\sigma = 0.1 \text{ nC/m}^2$ on one side. How far apart are equipotential surface whose potential differ by 5 V ?

3. Two large, parallel conducting plates are 10 cm apart & have charges of equal magnitude & opposite sign on their facing surface. An electrostatic force of $3.9 \times 10^{-12} \text{ N}$ acts on one electron.

The electric potential at a point in a plate is given by $V = 2x^2 - 3y^2$. What are the magnitude & direction of electric field at the point?

$$d(\text{distance}) = \sqrt{x^2 + y^2} = \sqrt{3^2 + 2^2} = \sqrt{9 + 4} = \sqrt{13}$$

$$E = \frac{\Delta V}{d}$$

$$\text{where } x = 3 \text{ \& } y = 2$$

$$= 4(3) - 6(2)$$

$$= 12 - 12 = 0$$

$$\text{magnitude } E = \sqrt{12^2 + (-12)^2} = \sqrt{144 + 144} = \sqrt{288}$$

25/11/17 CONDUCTORS & CURRENT: ELECTRIC CURRENT, RESISTORS & RESISTANCE, ELECTRIC POWER.

Electric Current is the quantity of charges flow in a wire or in a conductor or in a circuit per second.

Conductor allows electric current to pass through them easily.

Insulator doesn't allow electric current to pass through them.

The gap b/w valence band & the Conductor band is called energy gap.



Super conductor offer ^{resistance} no ~~conductor~~ to the flow of current & the resistance is zero ohm.

$$\text{Electric Current} = \frac{q}{t} = \frac{q}{t}$$

$$q = it$$

electric current is measured in ampere.

Unit of Current (A) = $\frac{C}{s}$

$$1 \text{ ampere} = 10^{-9} \text{ A} / 10^{-3} \text{ mA}$$

$$i = \frac{dq}{dt}$$

$$dq = i dt$$

$$q = \int i dt$$

Current density is the quantity of charge ^{that passes} per unit area.

$$j = \frac{I}{\text{area}} \frac{A}{m^2}$$

* Lighter object has high density than heavier object.

Resistivity is define as the ratio of electric field per Current density. $\rho = \frac{E}{j}$ (Electric field / Current density)

$$= \frac{V}{L} = \frac{V}{L} = \frac{A}{I}$$

$$\frac{I}{A}$$

$$V \propto I$$

$$V = IR$$

$$P = \frac{RA}{L}$$

$$\text{Slope} = \frac{\Delta V}{\Delta I} = \rho$$

Resistance = $R \propto L$

$$\therefore \rho \propto \frac{1}{A}$$

$$R \propto \frac{1}{A}$$

$$R = \frac{\rho L}{A}$$

$$\therefore \rho = \frac{RA}{L}$$

Conductivity:-

$$\sigma = \frac{1}{\rho} \quad \text{unit } (\Omega^{-1} \text{m}^{-1})$$

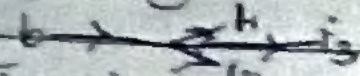
$$\rho = \frac{1}{\sigma}$$

$$\frac{I}{A} = \frac{E}{\rho l}$$

$$\Rightarrow J = \sigma E$$

Fixed resistor are resistor with ^{whole no} value. e.g 1, 2, 3, 4, 5, ... etc
 Variable resistor are resistor ^{no} which resistance can be varied.

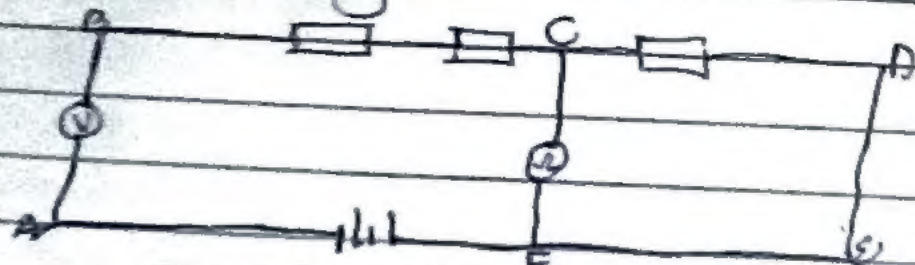
Arrangement of resistors:- Series & parallel.



$$I_0 = I_1 + I_2 + I_3$$

$$\text{or } I_0 - I_1 - I_2 - I_3 = 0$$

Series arrangement:



Group 1 = A B C F A

Group 2 = C A E F C

Group 3 = A B C D E F

$$V_1 = IR_1$$

$$V_2 = IR_2$$

$$V_3 = IR_3$$

$$V = V_1 + V_2 + V_3$$

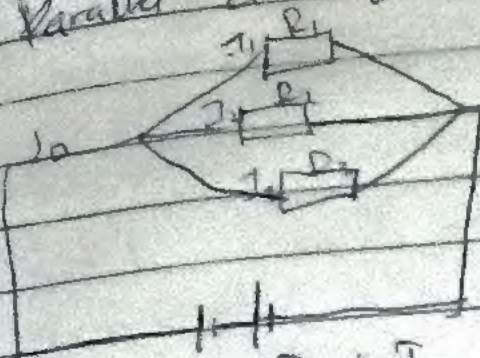
$$IR = IR_1 + IR_2 + IR_3$$

$$IR = I(R_1 + R_2 + R_3)$$

Combine resistance, equivalent resistance or total resistance

$$R_T = R_1 + R_2 + R_3$$

Parallel arrangement of resistors



$$I_0 = I_1 + I_2 + I_3$$

$$V = I R_1 \Rightarrow I = \frac{V}{R_1}$$

$$V = I_1 R_1 \Rightarrow I_1 = \frac{V}{R_1}$$

$$V = I_2 R_2 \Rightarrow I_2 = \frac{V}{R_2}$$

$$V = I_3 R_3 \Rightarrow I_3 = \frac{V}{R_3}$$

$$V = I R$$

$$I = \frac{V}{R}$$

$$\frac{V}{R_T} = \frac{V}{R_1} + \frac{V}{R_2} + \frac{V}{R_3}$$

$$V \left(\frac{1}{R_T} \right) = V \left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right)$$

$$\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

* Electric Conductance

Joule's law of Electric Current

$$H \propto I^2$$

$$H \propto R$$

$$H = I^2 R t$$

$$\text{Power} = I V = I(I R) = I^2 R$$

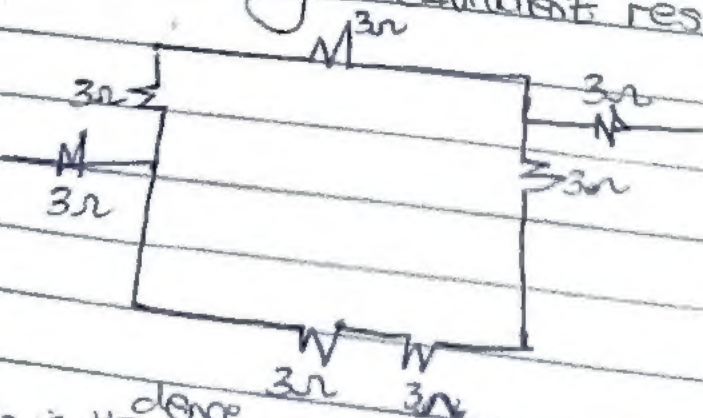
$$P = I V$$

$$I = \frac{V}{R} = \frac{V}{R} \times V = \frac{V^2}{R}$$

Example 1 A square block of alloy has dimensions 1.5cm by 1.5cm by 1.5cm. A potential difference is to be applied between the alloy block and a equipotential surfaces, take resistivity to be $9.6 \times 10^{-6} \Omega \text{m}$.

2. The resistivity of a broken piece of broken wire of length 30m is $5.4 \times 10^{-2} \Omega \text{m}$, if the cross sectional area of the wire is $9.5 \times 10^{-3} \text{m}^2$, Cal. the resistance of the wire.

3. ^A Determine resistivity or equivalent resistance of the circuit below



R_2 is the same as R_3

$$R_{11} = 3\Omega + 3\Omega = 6\Omega$$

R_4, R_5 & R_6 are in series

$$R_{12} = R_4 + R_5 + R_6$$

$$= 3\Omega + 3\Omega + 3\Omega = 9\Omega$$

$$\therefore R_{11} // R_{12}$$

$$= \frac{1}{R_{12}} = \frac{1}{R_{11}} + \frac{1}{R_{12}} = \frac{1}{6} + \frac{1}{9}$$

$$= \frac{3+2}{18} = \frac{5}{18}$$